## Sadhana Education Society

# L.S. RAHEJA <br> COLLEGE OF ARTS \& COMMERCE, SANTACRUZ (W), MUMBAI - 400054. 

## STATISTICS I (FYBA) TUTORIAL WORKBOOK

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# DEPARTMENT OF MATHEMATICS, STATISTICS \& COMPUTERS 

## STATISTICS I

## TUTORIAL WORKBOOK

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## Why this tutorial handbook is introduced?

"Mathematics is not about numbers, equations, computations or algorithms: it is about understanding."

William Paul Thurston

"Statistics is the grammar of science."
Karl Pearson

## The Field of Statistics

The field of statistics is the science of learning from data. Statisticians offer essential insight in determining which data and conclusions are trustworthy. Statisticians know how to solve scientific mysteries and how to avoid traps that can trip up investigators.

When statistical principles are correctly applied, statistical analyses tend to produce accurate results. What's more, the analyses even account for real-world uncertainty in order to calculate the probability of being incorrect.

To produce conclusions that you can trust, statisticians must ensure that all stages of a study are correct. Statisticians know how to:

- Design studies that can answer the question at hand
- Collect trustworthy data
- Analyze data appropriately and check assumptions
- Draw reliable conclusions

It has been observed that students enrolling for F.Y.B.A lack basics of Mathematics and Statistics as some of them did not opt for Statistics in F.Y.J.C and S.Y.J.C, due to which they lose connect with mathematical concepts and rigour.

To boost the confidence of students and to make them understand Statistics lessons taught in the class and to provide them hand on practice of standard questions this tutorial handbook has been introduced.

This tutorial handbook contains:
$\checkmark$ Latest Syllabus of Statistical techniques paper.
$\checkmark$ Paper Pattern
$\checkmark$ Reference Books
$\checkmark$ Unit wise questions for practice with enough space to solve them
$\checkmark$ Graph Papers

We hope this handbook will inculcate the problem solving aptitude among students and remove their Mathematics and Statistics phobia.

## SYLLABUS FOR STATISTICS AT FYBA

## Why Revision?

There is a Rapid expansion of knowledge in subject matter areas and improved instructional method during last decade. There are considerable curricular revisions happening at the high school level. Application of Mathematics and Statistics are widely used in industry and business. Keeping this in mind, a revision of syllabus required in accordance with the growth of subject of at the high school level and emerging needs of industry and its application.

## Objective:

The main objective of this course is to introduce mathematics and statistics to undergraduate students of commerce, so that they can use them in the field of commerce and industry to solve the real life problems.

Distribution of topics and lectures

| SEMESTER I Course Code | Credits |
| :--- | :--- |
| Statistics I | 2 Credits <br> (45 lectures <br> ) |
|  |  |
| Unit I: Types of data and data condensation: Population, Sample, SRS, <br> SRSWR, SRSWOR, types of scales, primary and secondary data, tabulation, <br> Association of attributes, Yule's coefficient of association, Yule's coefficient of <br> colligation. | 15 Lectures |
| Unit II: Classification of data and measures of central tendency: Univariate <br> frequency distribution, Bivariate frequency distribution, Cumulative frequency <br> distribution, Graphical representation, Histogram, frequency polygon, Ogives, <br> Steam and leaf diagram. <br> Measures of central tendency: Requirement of good measure, Median, Mode, <br> Partition Values, AM, GM, HM, Empirical relation between Mean, median and <br> mode, Merits and demerits. | 15 Lectures |

## Assessment of Practical Core Courses Per Semester per course:

1. Semester work, Documentation, Journal $\qquad$ 10 Marks.
2. Semester End Practical Examination $\qquad$ 40 Marks

## Semester End Examination Theory:

At the end of the semester, Theory examination of three hours' duration and 100 marks based on the three units shall be held for each course. Pattern of Theory question paper at the end of the semester for the course:

There shall be Five Questions of twenty marks each.
Question 1 based on all Three units. Ten sub-questions of two marks each.
Question 2 based on Unit I (Attempt any TWO out of THREE)
Question 3 based on Unit II (Attempt any TWO out of THREE)
Question 4 based on Unit III (Attempt any TWO out of THREE)
Question 5 based on all Three Units combined. (Attempt any TWO out of THREE)

## Practicals:

At the end of the semester, Practical examination of $\mathbf{2}$ hours' duration and 40 marks shall be held for the course. Marks for term work in each paper should be given out of 10. ( 5 for viva and 5 for journal)

Pattern of Practical question paper at the end of the semester for each course:
There shall be Four Questions of ten marks each. Students should attempt all questions.
Question 1 based on Unit I,
Question 2 based on Unit II,
Question 3 based on Unit III,
Question 4 based on all Three Units combined.
Students should attempt any two sub questions out of the three in each Question.

Workload Theory: 3 lectures per week per course.
Practicals: 3 lecture periods per course per week per batch.

## Descriptive Statistics - I

## Unit I: Types of data and Data condensation

## Q. 1. Answer the following questions

1. What are the merits and demerits of Tables?
2. Discuss the importance of classification in statistical analysis.
3. Write a short note on Association of attributes.
4. Write a short note on Measures of association.
5. What is contingency table? Give contingency tables for two attributes and three attributes.

## Q. 2. Solve following problems:

1. The weights in kg of 30 workers in a factory are as follows:
$61.4,67.0,56.2,71.0,64.0,69.0,63.5,63.0,62.4,72.5,61.2,64.5,58.5$, $62.1,64.0,69.5,58.0,63.2,50.0,60.8,64.5,60.0,57.5,62.5,57.6,62.5$, 68.4, 52.6, 59.5, 63.0

Classify and tabulate the data.
2. The marks obtained by 50 students of a class in a test are as follow:
$\begin{array}{llllllllll}26 & 49 & 33 & 42 & 53 & 35 & 47 & 39 & 61 & 43\end{array}$
$4431 \quad 594325 \quad 5245394857$
$\begin{array}{llllllllll}52 & 68 & 47 & 38 & 33 & 43 & 45 & 29 & 46 & 37\end{array}$
$\begin{array}{lllllllll}34 & 44 & 28 & 54 & 48 & 36 & 42 & 57 & 36 \\ 49\end{array}$
$\begin{array}{lllllllll}32 & 43 & 59 & 47 & 27 & 51 & 38 & 69 & 64 \\ 57\end{array}$
Classify the data taking C.I. 20-29, 30-39, 40-49, 50-59, 60-69
3. Convert the class intervals $10-18,20-28,30-38,40-48$ into exclusive type.
4. The marks obtained by 100 students of a class in a certain subject are given below:

| Marks | $20-30$ | $30-40$ | $40-50$ | $50-60$ | $60-70$ | $70-80$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| No. of students | 8 | 20 | 30 | 24 | 12 | 6 |
| a) | Prepare Less than cumulative frequency table. |  |  |  |  |  |
| b) | Prepare More than cumulative frequency table |  |  |  |  |  |
| c) | Construct Histogram, frequency polygon, frequency <br> curve, Ogives |  |  |  |  |  |
| d) | Find the graphical value of mode. |  |  |  |  |  |

5. Construct relative frequency table for the data
x: $\begin{array}{llllll} & 1 & 2 & 3 & 4\end{array}$
f: $2 \begin{array}{lllll}5 & 11 & 6 & 1\end{array}$
6. The following data gives the age in years $0 f 60$ staff member in an office. Prepare the relative frequency table.

| Age in years | $20-30$ | $30-40$ | $40-50$ | $50-60$ | $60-70$ |
| :--- | :---: | :---: | :---: | :---: | :---: |
| No. of students | 7 | 15 | 20 | 12 | 6 |

7. $\mathrm{N}=450,(\mathrm{~A})=265,(\mathrm{~B})=242,(\mathrm{C})=250,(\mathrm{AB})=135,(\mathrm{AC})=132,(\mathrm{BC})$ $=144,(A B C)=88$. Find the other class frequencies.
8. From the following data find the remaining frequencies. In a survey of 400 people it was observed out of 84 lefties there were 48 males. In all there were 160 females.
9. From the following data find coefficient of association between Inoculation and affection.

|  | Affected | Not Affected |
| :---: | :---: | :---: |
| Inoculated | 12 | 26 |
| Non-Inoculated | 16 | 6 |

Unit II: Classification of data \& measures of Central Tendency
Q. 1. Define the following terms with one example:

1. Class interval

## 2. Class width

## 3. Exclusive class interval

4. Inclusive class interval
5. Open end class intervals
6. Class limits
7. Class boundaries
8. Class mark
9. Relative frequency distribution
10.Cumulative frequency distribution
11.Arithmetic mean
12.Weighted mean

## 13.Median

14. Mode

## Q. 2. Answer the following questions.

1. Write a short note on Frequency distribution for discrete variable and continuous variable.
2. What is the cumulative frequency distribution? What are it's types.?
3. What are the advantages and disadvantages of graphs?
4. What are the requisites of good measures of central tendency?
5. How a mode can be located graphically by using Histogram?
6. Explain the mathematical relation between Mean, Mode and Median.
Q. 3. Write a short note on:
7. Histogram
8. Frequency Polygon
9. Frequency Curve
10. Ogives
11. Steam and leaf diagram
12. Types of Measures of central tendency

## Q. 4. Solve following problems:

1. The following data gives distribution of income tax paid by 500 employees of a company.
Find
i. $\quad \mathrm{Q}_{1}, \mathrm{Q}_{3}$, Quartile Deviation.
ii. Standard Deviation.
iii. Variance.
iv. Coefficient of variance.

| $03-04$ | $04-05$ | $05-06$ |
| :---: | :---: | :---: |


| 7 | 07-08 | 08-09 | 09 |
| :---: | :---: | :---: | :---: |

2. Calculate Standard deviation, Variance, $\mathrm{D}_{4}, \mathrm{D}_{7}, \mathrm{P}_{60} \& \mathrm{P}_{30}$ from the following data.

| Marks | 20 | 25 | 30 | 35 | 45 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| No. of students | 5 | 14 | 20 | 11 | 10 |

3. A hospital has collected data regarding number of days spent in hospital for a particular disease. Calculate the arithmetic mean for number of days spent in the hospital.

| No. of days spent | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| No. of patients | 5 | 6 | 5 | 10 | 8 | 4 | 3 | 2 |

4. Find the arithmetic mean, median and mode for the following data, representing marks of 80 students.

| Marks | $0-10$ | $10-20$ | $20-30$ | $30-40$ | $40-50$ |
| :--- | :---: | :---: | :---: | :---: | :---: |
| No. of students | 12 | 13 | 21 | 19 | 15 |

5. The following data gives the consumption of electricity. Find the average consumption.

| No. of units | $0-200$ | $200-$ <br> 400 | $400-$ <br> 600 | $600-$ <br> 800 | $800-$ <br> 1000 | $1000-$ <br> 2000 | $1200-$ <br> 1400 |
| :--- | ---: | :--- | :--- | :--- | :--- | :--- | :--- |
| No. of <br> consumers | 9 | 18 | 27 | 35 | 32 | 28 | 11 |

6. The following frequency distribution represents weights in grams of mangoes of a given variety, in a box. Find the average weight of mangoes.

| Weight in <br> gms | $410-$ <br> 419 | $420-$ <br> 429 | $430-$ <br> 439 | $440-$ <br> 449 | $450-$ <br> 459 | $460-$ <br> 469 | $470-$ <br> 479 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No. Of <br> mangoes | 14 | 20 | 42 | 54 | 45 | 18 | 7 |

7. Find the range and median for the followings sets of observation $53,43,30,55,75,50,32,39,62$.
8. Find the median for the followings data representing the age in the year of children.

| Age in the years | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| No. of children | 14 | 20 | 40 | 54 | 40 | 18 | 7 | 7 |

9. Following are the marks of the 15 students in a certain test. Find the modal marks. $18,22,25,42,39,35,25,33,34,25,29,37,35,25$ and 40.
10.Find the mode of the following data, representing size of readymade pants.

| Size of pants in cms | 60 | 65 | 70 | 75 | 80 | 85 | 90 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| No. of pants | 11 | 15 | 25 | 40 | 20 | 15 | 10 |

11.The following data gives frequency distribution of marks of some students. The average marks are 33 . Using this find the numbers of students with marks between 40 and 50.

| Marks | $0-10$ | $10-20$ | $20-30$ | $30-40$ | $40-50$ | $50-60$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| No. of students | 5 | 10 | 25 | 30 | --- | 10 |

Unit III: Measures of Dispersion, Skewness \& Kurtosis
Q. 1. Define the following terms with one example:

1. Range
2. Coefficient of range
3. Quartile deviation
4. Coefficient of quartile definition
5. Mean deviation
6. Coefficient of variation

## Q. 2. Answer the following questions.

1. What are the requisites of good measures of dispersion?
2. Define standard deviation as measure and the corresponding relative measure of dispersion.
3. Explain the effect of change of origin and scale on standard deviation.

## Q. 3. Write a short note on:

1. Explain the difference between Absolute measures of dispersion and relative measures of dispersion.
2. State and prove properties of variance.

## Q. 4. Solve the following problems:

1. The following data gives distribution of income tax paid by 500 employees of a company. Find
v. $Q_{1}, Q_{3}$, Quartile Deviation.
vi. Standard Deviation.
vii. Variance.
viii. Coefficient of variance.

| Income Tax (Rs.'000) | $03-04$ | $04-05$ | $05-06$ | $06-$ <br> 07 | $07-08$ | $08-09$ | $09-10$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No of employees | 40 | 60 | 80 | 120 | 100 | 60 | 40 |

2. Calculate Standard deviation, Variance, $\mathrm{D}_{4}, \mathrm{D}_{7}, \mathrm{P}_{60} \& \mathrm{P}_{30}$ from the following data.

| Marks | 20 | 25 | 30 | 35 | 45 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| No. of students | 5 | 14 | 20 | 11 | 10 |

